

# A New Modulation Method based on Switching Losses Minimization for DC-AC Inverters

Victor Truong Thinh Lam, Georgios Papafotiou, Tobias Geyer



Power Electronics & Energy Storage event  
27 juni 2023 | 1931 Congrescentrum 's-Hertogenbosch

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# What I will talk about ...

- Multilevel DC-AC inverters
- Preliminaries
- Proposed modulation method
- Simulation results
- Conclusion

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# Multilevel DC-AC inverter

Many *applications*:

- photovoltaic systems
- high-voltage power transmissions
- electric motor drives

Characteristics:

- Controlled AC *voltage source*
  - composed of >2 levels
  - drives desired load currents



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# Three-level NPC inverter

- Applications of few MW and kV

- Phase voltages

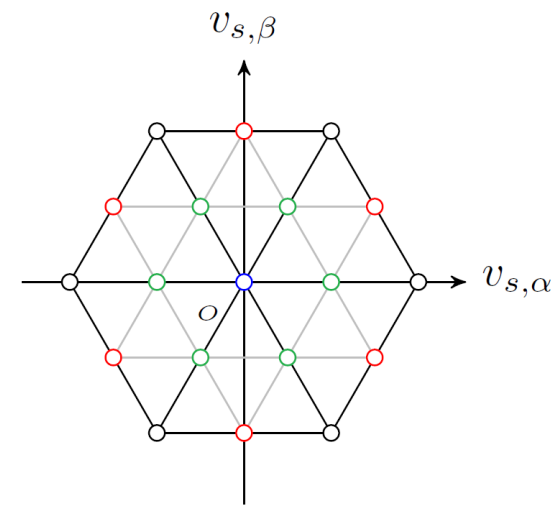
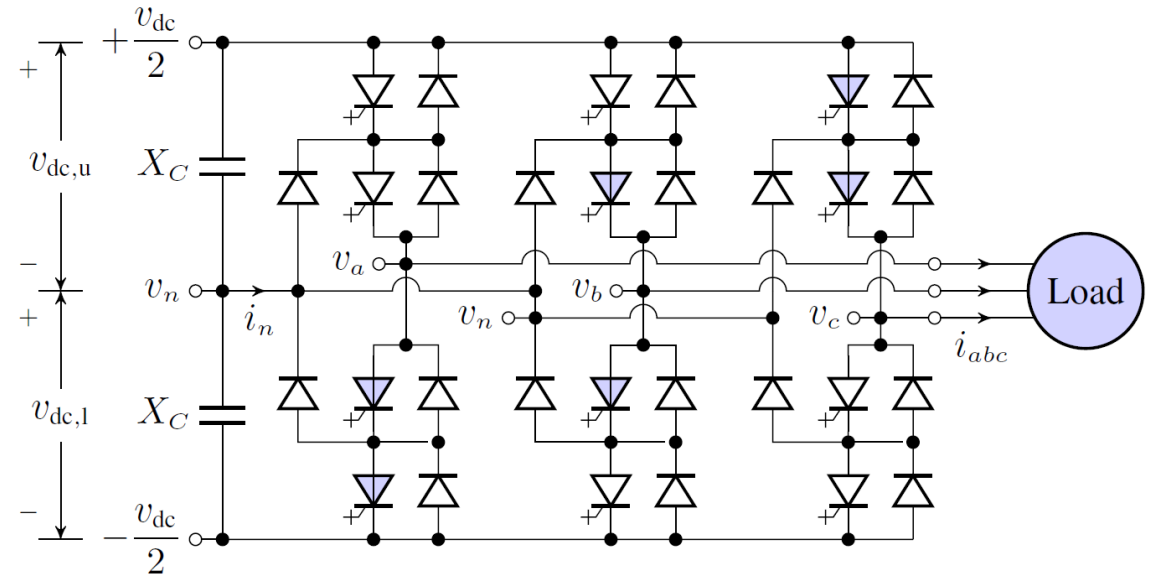
$$v_x = \{-v_{dc,l}, v_n, v_{dc,u}\}$$

- 27 switch positions

$$u_{abc} = \{-1, 0, 1\}^3$$

- **Clarke** transformation:

$$v_{\alpha\beta} = P v_{abc}, \text{ where } P = \frac{2}{3} \begin{bmatrix} 1 & -\frac{1}{2} & -\frac{1}{2} \\ 0 & \frac{\sqrt{3}}{2} & -\frac{\sqrt{3}}{2} \end{bmatrix}$$



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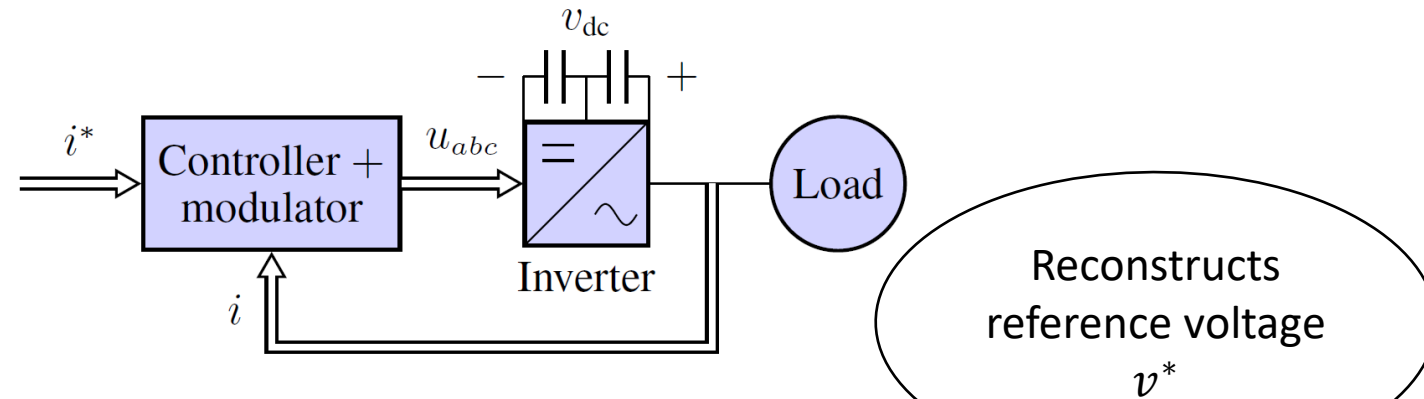
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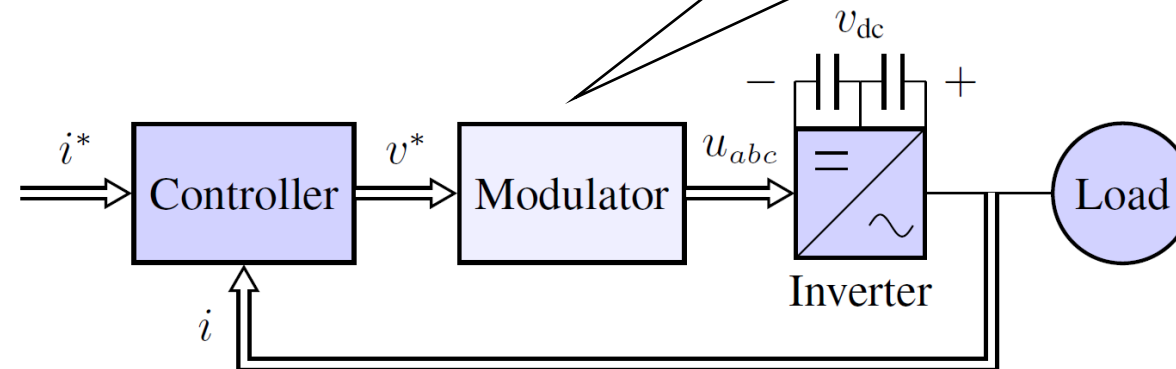
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# Load current control schemes

- **Direct** control:



- **Indirect** control:



# Trade-off switching losses and THD

- Direct control: *trade-off*
- Indirect control: so far *performance* and *constraint* satisfaction
  - *Trade-off* done by modulator → focus of this presentation
- Modulators (implicit trade-off):
  - *Soft switching type* modulation (switches around zero currents)
  - *Discontinuous PWM* (reduces number of switchings)
  - *Space vector modulation* (small voltage jumps)

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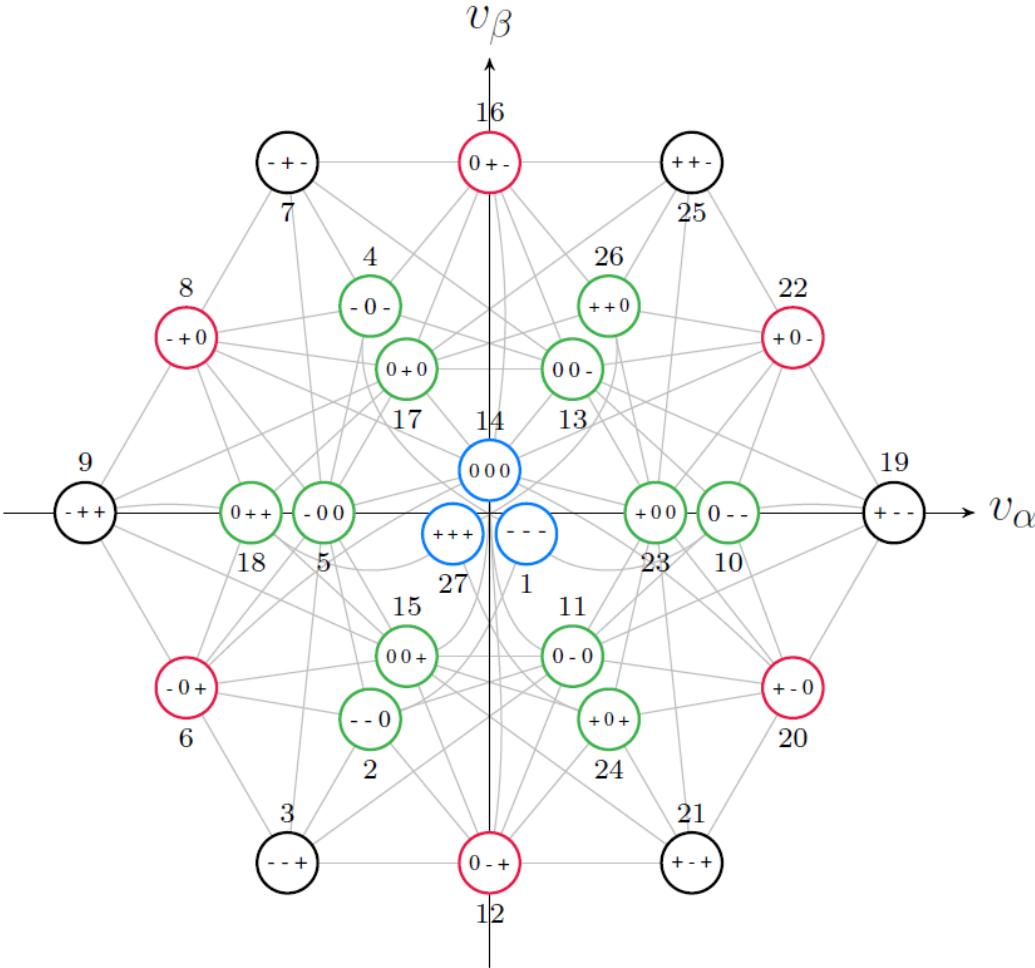
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# Three-level NPC inverter

- Switching *constraints*
  - Not directly between -1 and 1
  - In max 2 phase, in opposite inverter halves
- Neutral-point voltage *balancing*



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# Space vector modulation

- The *closest* triangle with  $v_1, v_2, v_3$

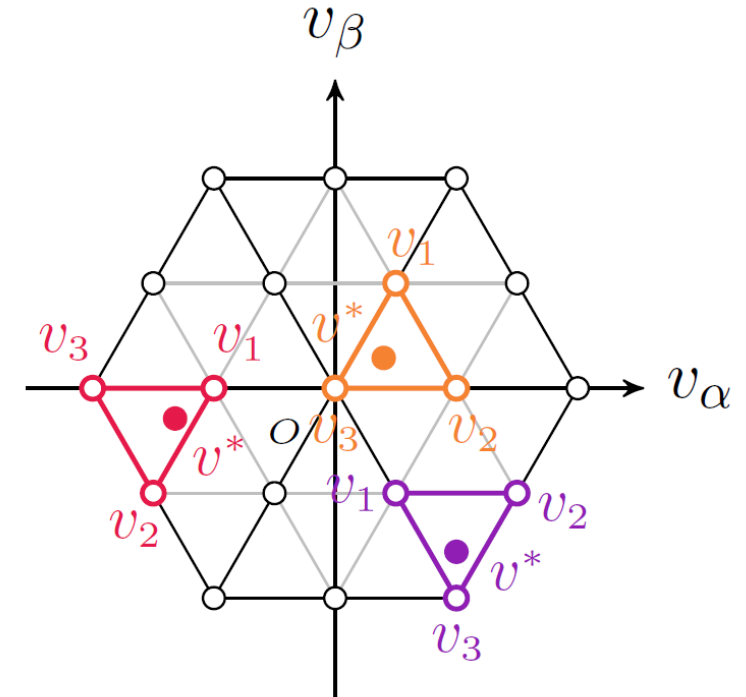
- For every *modulation cycle*  $T_s$ :

$$t_1 v_{1,\alpha} + t_2 v_{2,\alpha} + t_3 v_{3,\alpha} = T_s v_\alpha^*$$

$$t_1 v_{1,\beta} + t_2 v_{2,\beta} + t_3 v_{3,\beta} = T_s v_\beta^*$$

$$t_1 + t_2 + t_3 = T_s$$

- $t_1, t_2, t_3 \geq 0$



# Space vector modulation

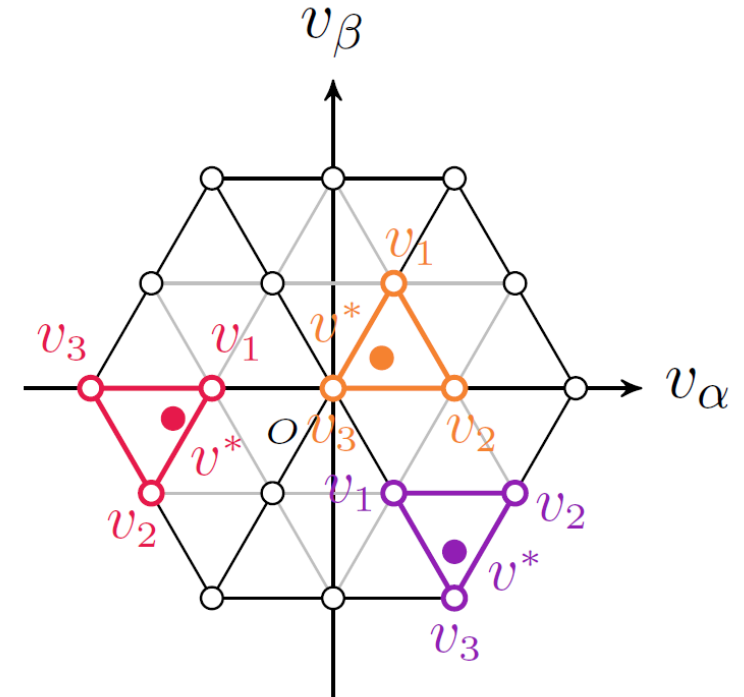
- The *closest* triangle with  $v_1, v_2, v_3$
- Define  $\bar{t} = \frac{t}{T_s}$ , for every *modulation cycle*  $T_s$ :

$$\bar{t}_1 v_{1,\alpha} + \bar{t}_2 v_{2,\alpha} + \bar{t}_3 v_{3,\alpha} = v_\alpha^*$$

$$\bar{t}_1 v_{1,\beta} + \bar{t}_2 v_{2,\beta} + \bar{t}_3 v_{3,\beta} = v_\beta^*$$

$$\bar{t}_1 + \bar{t}_2 + \bar{t}_3 = 1$$

- $\bar{t}_1, \bar{t}_2, \bar{t}_3 \geq 0$



# What I will talk about ...

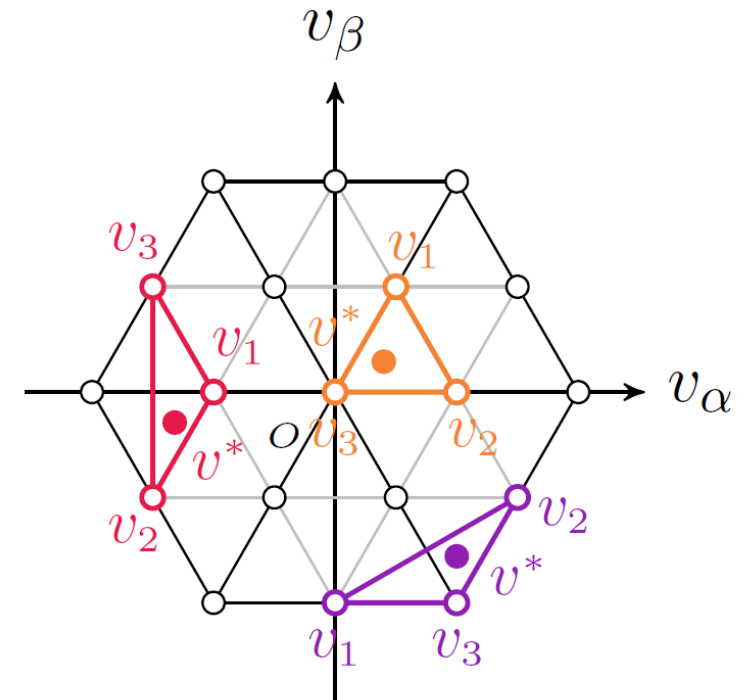
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# Proposed modulation method

- *Online adaptive* SVM
- Geometrically, *any* triangle (convex combination) containing  $v^*$  possible instead of the *closest* one
- The *voltage* and *current paths*

$$V^* = \begin{bmatrix} v_1^* \\ \vdots \\ v_L^* \end{bmatrix} \text{ and } I = \begin{bmatrix} i_1 \\ \vdots \\ i_L^* \end{bmatrix}$$



- The *'best'* triangle chosen that improves loss-THD trade-off

# Proposed modulation method (cont'd)

- *Optimization* window  $L$
- For each  $p$ -th modulation cycle  $T_s$ ,

$$f_p = w_{loss,p} \left( \sum_{q=1}^3 \sum_{r=a,b,c} E_{p,q,r} \right)^2 + w_{THD,p} \left( \sum_{q=1}^3 e_{p,q,\alpha}^2 + e_{p,q,\beta}^2 \right)$$

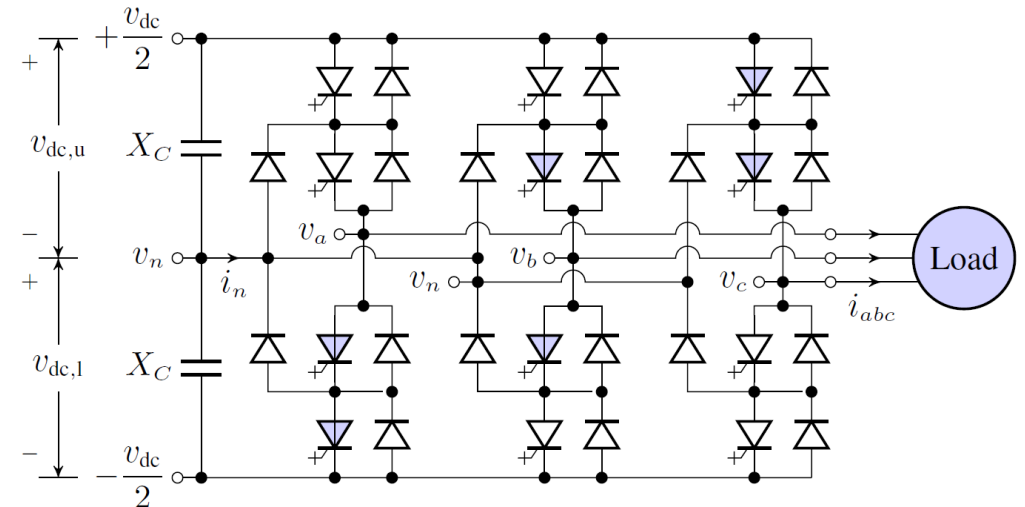
- Choose switching sequence which *minimizes*  $f = \sum_{p=1}^L f_p$

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# Neutral-point voltage balancing

- How does neutral-point *voltage* behave?

$$\frac{dv_n}{dt} = -\frac{1}{2X_C} i_n$$



- Neutral-point *current* drawn only if phase connected to neutral-point

$$i_n = (1 - |u_a|)i_a + (1 - |u_b|)i_b + (1 - |u_c|)i_c$$

- Predict using *forward Euler*  $v_n(t + \Delta t) = v_n(t) + \Delta t \cdot -\frac{1}{2X_C} i_n$

# Proposed modulation method (cont'd)

- *Optimization* window  $L$
- For each  $p$ -th modulation cycle  $T_s$ ,

$$f_p = w_{loss,p} \left( \sum_{q=1}^3 \sum_{r=a,b,c} E_{p,q,r} \right)^2 + w_{THD,p} \left( \sum_{q=1}^3 e_{p,q,\alpha}^2 + e_{p,q,\beta}^2 \right) + w_{v_n,p} v_{n,p}^2$$

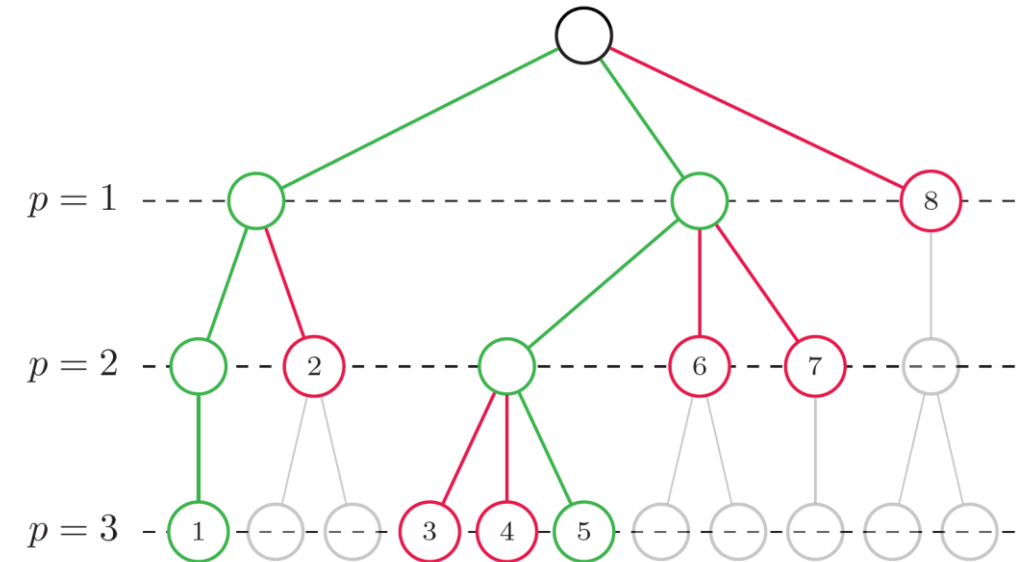
- Choose switching sequence which *minimizes*  $f = \sum_{p=1}^L f_p$
- Weights depend whether  $v_{n,p}$  within *bounds*

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# Proposed modulation method (cont'd)

- *Integer* optimization problem
- $3L$  decision variables, each with 27 vectors, so  $27^{3L}$  *possible combinations*
- Solved using *branch and bound* method
- Every *node* represents a triangle (3 vectors)

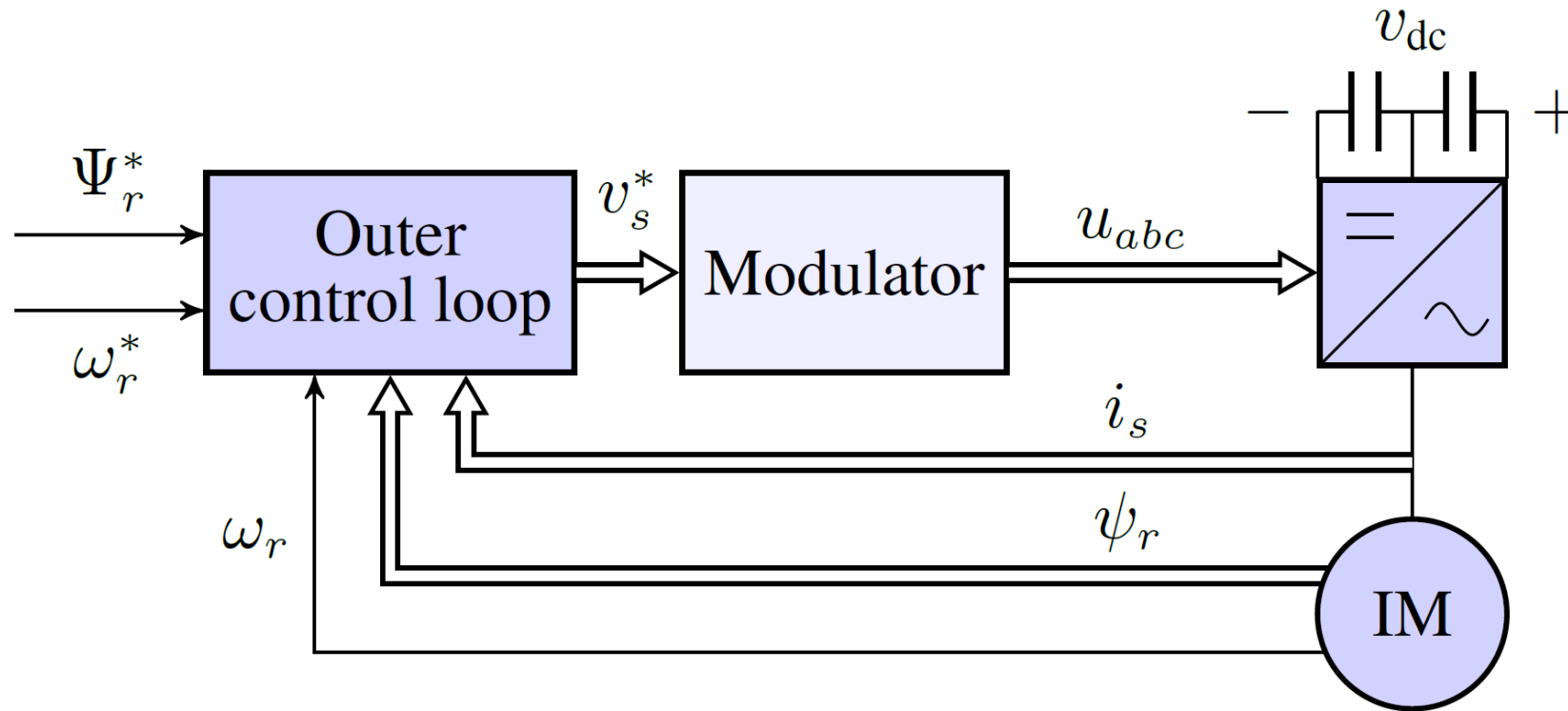


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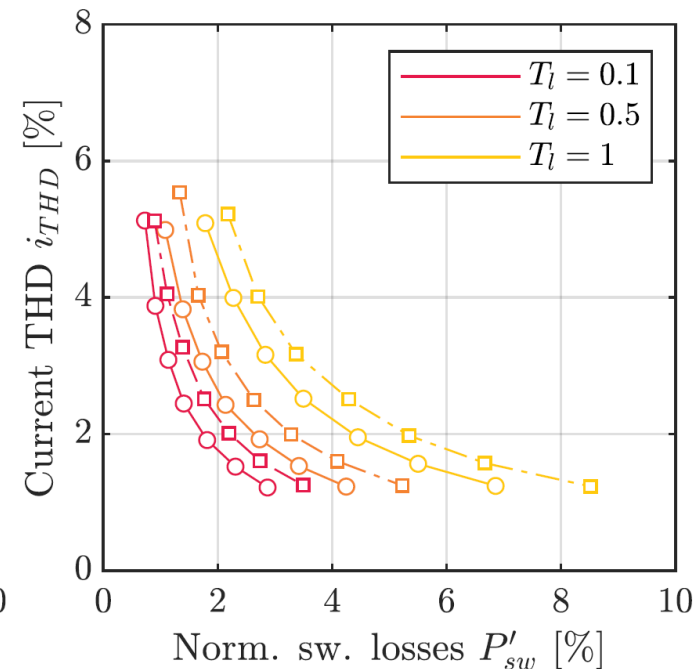
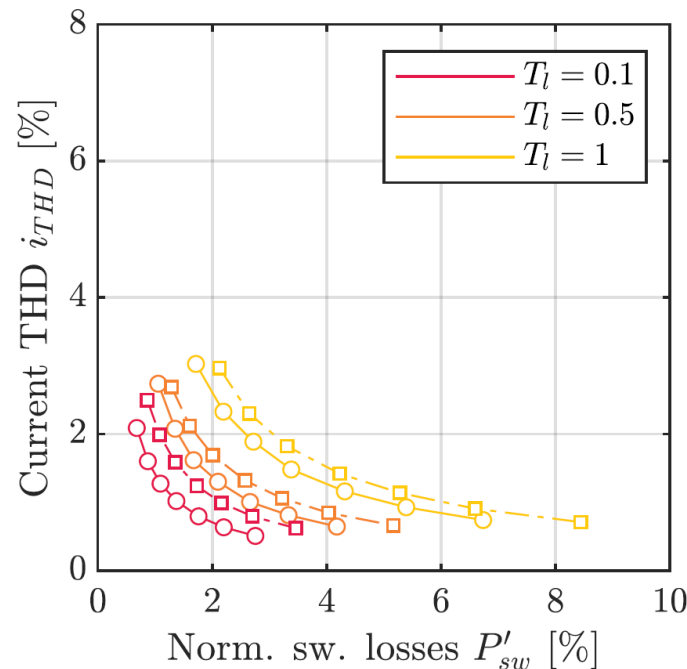
# Field-oriented control



# Loss-THD trade-off

- *SVM* (dash-dotted squares) vs *oaSVM* (solid circles)
- For  $L = 1$ , *speed*  $\omega_r = 0.1$  pu (left) and  $\omega_r = 0.4$  pu (right),

Parameter	Value
$w_{loss}$	1
$w_{THD}$	320
$w_{v_n}$	$1 \cdot 10^9$
$v_{n,min}$	-0.04 pu
$v_{n,max}$	0.04 pu



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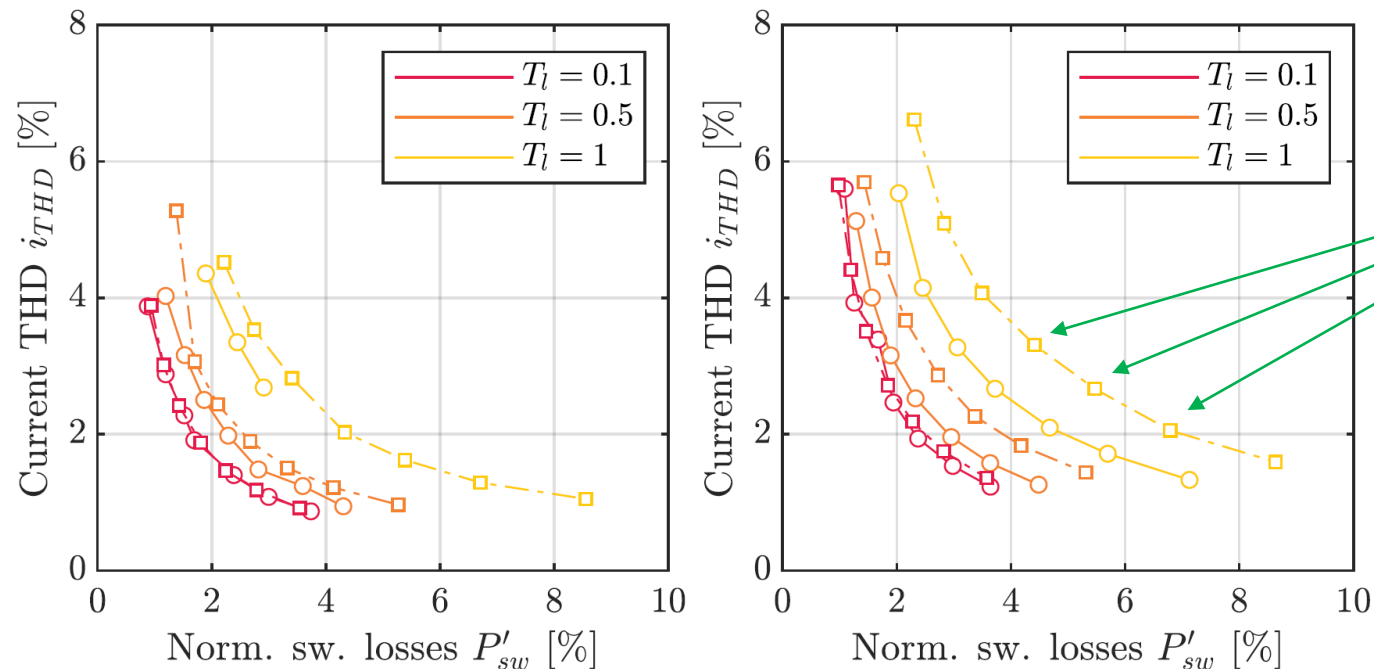
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# Loss-THD trade-off (cont'd)

- *SVM* (dash-dotted squares) vs *oaSVM* (solid circles)
- For  $L = 1$ , *speed*  $\omega_r = 0.7$  pu (left) and  $\omega_r = 1$  pu (right)
- Same *parameters* as before
- *Infeasibility* solvable using longer optimization windows



Losses reduced by **29.5%** for same THD for  $T_l = \omega_r = 1$  pu

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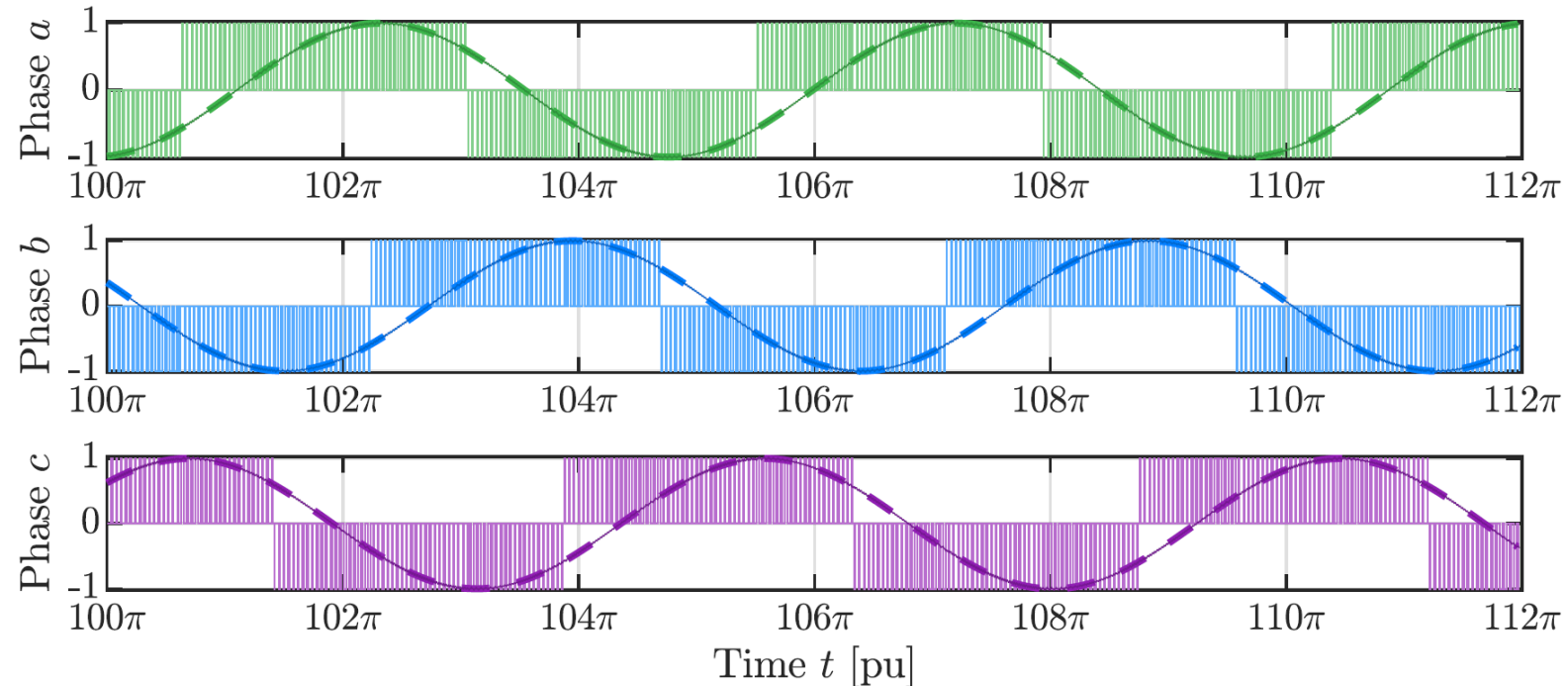
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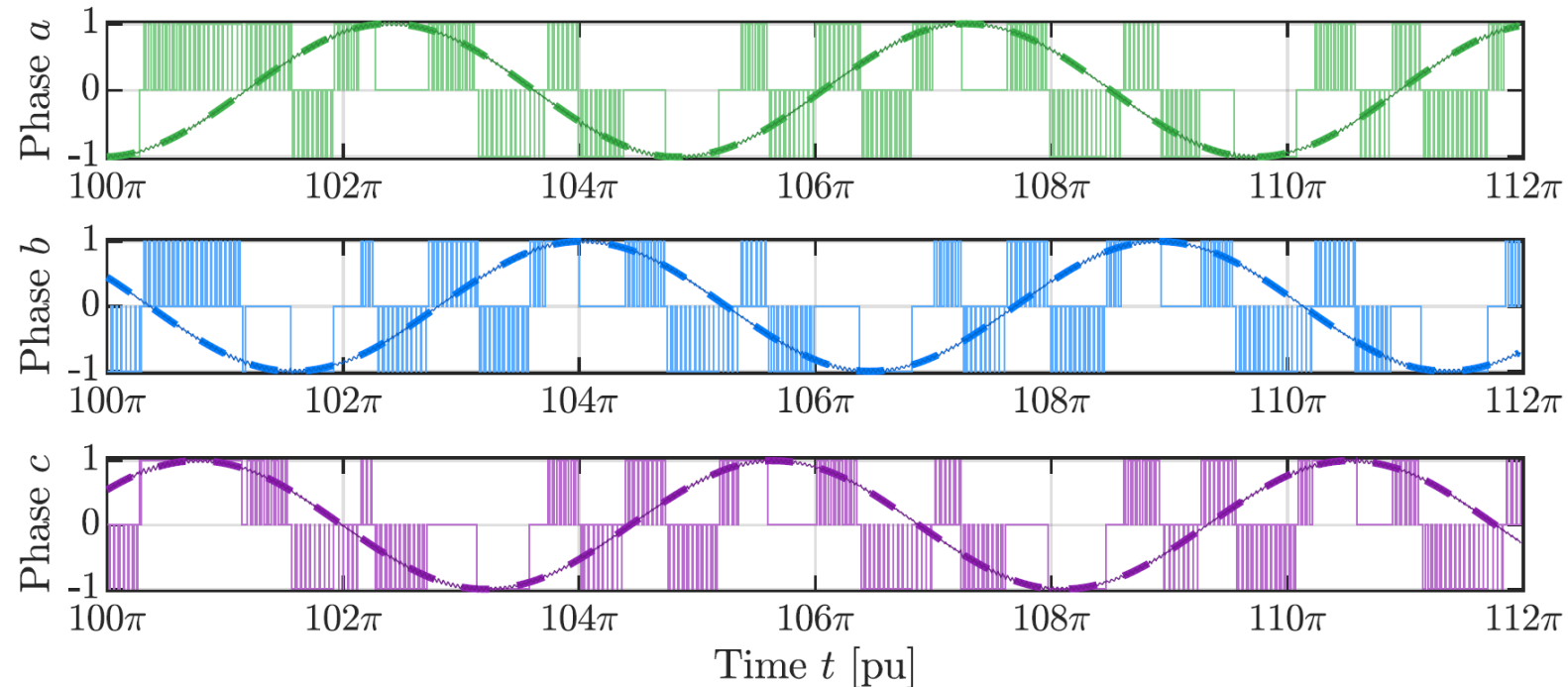
# Space vector modulation

- For *speed*  $\omega_r = 0.4$  pu, *load*  $T_l = 1$  pu
- Same *parameters* as before



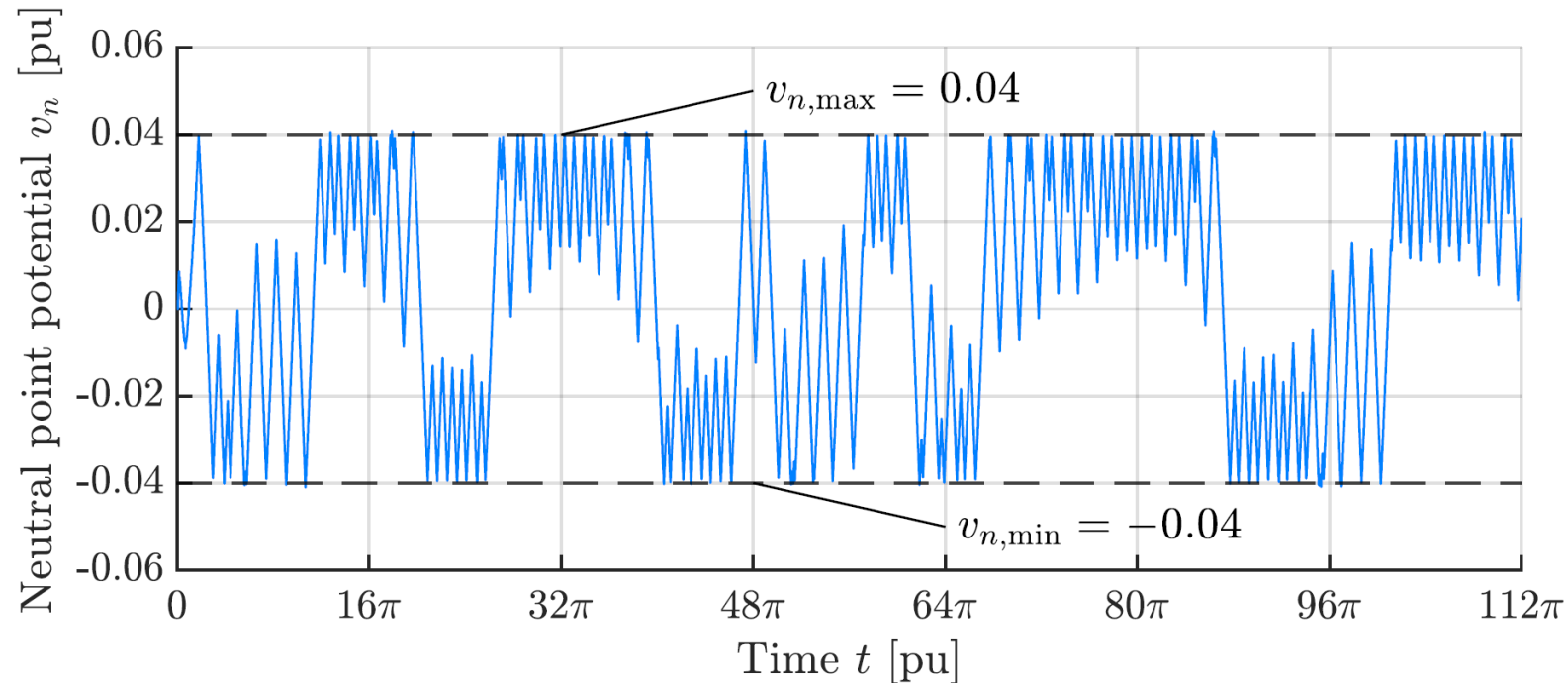
# Online adaptive SVM

- For *speed*  $\omega_r = 0.4$  pu, *load*  $T_l = 1$  pu
- Same *parameters* as before
- *Clamps* at high currents, similar to discrete PWM



# Online adaptive SVM (cont'd)

- For *speed*  $\omega_r = 0.4$  pu, *load*  $T_l = 1$  pu
- Same *parameters* as before





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# Conclusion

## Summary

- New modulation method *online adaptive SVM*
- Blend of *SVM* and discrete PWM, very flexible
- Improves *trade-off* between losses and THD
- Balances *neutral-point voltage* within bounds
- *Infeasibility* solvable for longer optimization windows
- High computational complexity, *brand and bound* method

## Future work:

- Investigate longer *optimization window*  $L > 1$
- Explore other *cost functions*

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# Thank you for your attention!

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The logo for TU/e, consisting of the letters 'TU' in a bold, red, sans-serif font, followed by a red diagonal slash and a lowercase 'e' in the same font.

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A graphic element for the Energy Storage section, featuring a horizontal line that transitions into a series of green lines that fan out to the right, ending in small plus signs.